

# Effect of non-Gaussian fluctuations on the spreading time of a SWIR epidemic model.

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A few years ago, there happened a big controversy on the scaling behavior of the golden time required to reach a entire outbreak on inter-dependent (ID) networks. At the transition point, the average cascade time  $\langle t_c \rangle$  scales with the system size  $N$  as  $\langle t_c \rangle \sim N^\zeta$ . The exponent  $\zeta$  was a controversial issue. It was argued in Zhou *et al.* (PRE 90, 012803)  $\zeta = 1/4$ . On the other hand, in Grassberger (PRE 91, 062806), it was argued that the exponent value  $\zeta = 1/4$  is incorrect, but rather 0.280 after extensive simulations. Resolution or even finding the origin of this discrepancy seemed to be difficult thus far.

In our study, we find that  $\zeta$  for several other cascade dynamics models such as SWIR model,  $k$ -core percolation, and the threshold model of Watts are also measured to be slightly larger than  $1/4$ . In the framework of SWIR model, which is also known as a generalized epidemic model, we found that non-Gaussian distribution of the finite-size fluctuation is majorly responsible for  $\zeta$  being larger than  $1/4$ . We also confirmed that this is true for the case of  $k$ -core percolation too. However, due to the decreasing asymmetry of the non-Gaussian distribution for larger systems, it remains open whether or not  $\zeta$  reduces to  $1/4$  in the asymptotically large- $N$  limit.  
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† Wonjun Choi, Deokjae Lee and B. Kahng, arXiv:1706.08968, (2018).